Strategic and Intensive Interventions in Mathematics - Part 1 of 2

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The Pennsylvania Training and Technical Assistance Network

#psychedaboutmath
Highlights:

Part 1
- Diagnostic Assessment for Intervention Selection
- Instructional Hierarchy
- Intensification and features of math interventions
- Acquisition Interventions

Part 2
- Fluency Interventions
- Progress Monitoring
- Decision Making
Let’s Stamp!
Let's practice!
What best describes your role? You may stamp more than one if it applies to you.

<table>
<thead>
<tr>
<th>Graduate Student</th>
<th>Higher Ed Faculty</th>
<th>K-12 School Psych Practitioner</th>
<th>Specialized Setting School Psych Practitioner</th>
<th>Administrator</th>
<th>Other</th>
</tr>
</thead>
</table>
Diagnostic Assessment

& Skill by Treatment interaction
**TYPES OF DIAGNOSTIC MEASURES FOR MATH**

### GENERAL OUTCOME MEASURE (GOM)*

Curriculum-Based Measurement - Computation or Math Concepts and Applications  *there really is not a great GOM in math like in reading*

### Skills-Based Measures

<table>
<thead>
<tr>
<th>Math Computation</th>
<th>Math Concepts and Applications</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Addition</strong></td>
<td>Early Numeracy (e.g., number sense)</td>
</tr>
<tr>
<td><strong>Subtraction</strong></td>
<td>Operations and algebraic thinking</td>
</tr>
<tr>
<td><strong>Multiplication</strong></td>
<td>Numbers and operations in base ten</td>
</tr>
<tr>
<td><strong>Division</strong></td>
<td>Measurement and data</td>
</tr>
<tr>
<td><strong>Quantitative Comparison 0-9</strong></td>
<td>Geometry</td>
</tr>
<tr>
<td><strong>Quantitative Comparison 9-19</strong></td>
<td>Numbers and operations-fractions</td>
</tr>
<tr>
<td><strong>Quantitative Comparison 10-20</strong></td>
<td>Expressions and equations</td>
</tr>
<tr>
<td><strong>Quantitative Comparison 101-999</strong></td>
<td></td>
</tr>
<tr>
<td><strong>Quantitative Comparison 1001-9999</strong></td>
<td></td>
</tr>
</tbody>
</table>

#### Subskill Mastery Measures

<table>
<thead>
<tr>
<th>Subskill Mastery Measures</th>
<th>Subskill Mastery Measures</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sums to 6</td>
<td>Fact Families Addition &amp; Subtraction 0-5</td>
</tr>
<tr>
<td>Sums to 12</td>
<td>Fact Families Addition &amp; Subtraction 0-9</td>
</tr>
<tr>
<td>Sums to 20</td>
<td>Fact Families Addition &amp; Subtraction 0-20</td>
</tr>
<tr>
<td>Subtraction 0-5</td>
<td>2-digit Addition without regrouping</td>
</tr>
<tr>
<td>Subtraction 0-9</td>
<td>2-digit Addition with regrouping</td>
</tr>
<tr>
<td>Subtraction 0-12</td>
<td>3-digit Addition without Regrouping</td>
</tr>
<tr>
<td>Subtraction 0-15</td>
<td>3-digit Addition with and without Regrouping</td>
</tr>
<tr>
<td>Subtraction 0-20</td>
<td>2-digit Subtraction without Regrouping</td>
</tr>
<tr>
<td>2-digit Subtraction 0-5</td>
<td>2-digit Subtraction with Regrouping</td>
</tr>
<tr>
<td>2-digit Subtraction 0-9</td>
<td>3-digit Subtraction without Regrouping</td>
</tr>
<tr>
<td>2-digit Subtraction 0-12</td>
<td>3-digit Subtraction with Regrouping</td>
</tr>
<tr>
<td>2-digit Subtraction 0-15</td>
<td>3-digit Subtraction with and without Regrouping</td>
</tr>
<tr>
<td>2-digit Subtraction 0-20</td>
<td>3-digit Addition &amp; Subtraction with and without Regrouping</td>
</tr>
</tbody>
</table>
**Sequence Skills**

What are the prerequisite skills?

Retention of previously learned skills improves when a small amount of material is presented at a time.

- What are the foundational skills?
- Too many skills or difficult tasks increase off-task behavior.

**Task Analyses**

How can the concepts be divided into smaller units?

Students learn each skill to mastery from the earliest unknown skill.

- Simpler skills + concepts come first

**Subskill Mastery**

As students master subskills, level of teacher help fades.

Match student performance to instructional hierarchy.

- Acquisition
- Fluency
- Maintenance/Generalization
Example of Sequence of Skills: Acadience Math (1st grade)

 Might we need to break down any of these skills into smaller units?

<table>
<thead>
<tr>
<th>Problem #</th>
<th>Problem Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1, 11</td>
<td>Add 0 or 1 to a one-digit number.</td>
</tr>
<tr>
<td>2, 15, 20, 22</td>
<td>Add two one-digit numbers, excluding 0 and 1.</td>
</tr>
<tr>
<td>3, 13</td>
<td>Subtract a one-digit number from a two-digit number (within 20) resulting in a</td>
</tr>
<tr>
<td></td>
<td>difference of 11 or more, without renaming.</td>
</tr>
<tr>
<td>4, 10, 21, 24</td>
<td>Subtract a one-digit number from a one-digit number, excluding 0 and 1 in the</td>
</tr>
<tr>
<td></td>
<td>subtrahend.</td>
</tr>
<tr>
<td>5, 17</td>
<td>Subtract a one-digit number from a two-digit number (within 20), resulting in a</td>
</tr>
<tr>
<td></td>
<td>difference of 9 or less.</td>
</tr>
<tr>
<td>6, 19</td>
<td>Subtract 0 or 1 from a one-digit number.</td>
</tr>
<tr>
<td>7, 12</td>
<td>Add a two-digit and a one-digit number, with renaming, resulting in a sum of 20.</td>
</tr>
<tr>
<td>8, 14</td>
<td>Subtract a one-digit number from 20, with renaming.</td>
</tr>
<tr>
<td>9, 16, 19, 23</td>
<td>Add a two-digit and a one-digit number, without renaming, resulting in a sum of 20</td>
</tr>
<tr>
<td></td>
<td>or less.</td>
</tr>
</tbody>
</table>
Where might I find a sequence of skills?
Check out: *CBA Manual* (Wright, Appendix D)

<table>
<thead>
<tr>
<th>M</th>
<th>I</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade 1</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1. Add two one-digit numbers: sums to 10.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2. Subtract two one-digit numbers: combinations to 10.</td>
<td></td>
</tr>
<tr>
<td>Grade 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>3. Add two one-digit numbers: sums 11 to 19.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>4. Add a one-digit number to a two-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>5. Add a two-digit number to a two-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>6. Add a three-digit number to a three-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>7. Subtract a one-digit number from a one- or two-digit number: combinations to 18.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>8. Subtract a one-digit number from a two-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>9. Subtract a two-digit number from a two-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>10. Subtract a three-digit number from a three-digit number--no regrouping.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>11. Multiplication facts--0's, 1's, 2's. column.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>20. Add a three-digit number to a three-digit number with regrouping from the units to the tens column only.</td>
<td></td>
</tr>
<tr>
<td></td>
<td>21. Add a three-digit number to a three-digit number with regrouping from the tens to the hundreds column only.</td>
<td></td>
</tr>
</tbody>
</table>

Adapted from Shapiro (1989)
### Sequence of Skills?

<table>
<thead>
<tr>
<th>Sums to 6</th>
<th>Sums to 12</th>
<th>Sums to 20</th>
<th>Subtraction 0-5</th>
<th>Subtraction 0-9</th>
<th>Subtraction 0-12</th>
<th>Subtraction 0-15</th>
</tr>
</thead>
</table>

Find out where **student is** ... find out where student **needs to be**.
Calculating DCPM

- Digits correct per minute can be used as a metric to score student mathematics performance (computation).

- Helps provide a consistent metric (vs. problems correct) to show incremental growth (e.g., student doesn’t understand concept of regrouping yet and gets 0 digits correct, but then learns how to regroup ones and gets partial digits correct in a 2-digit + 2-digit addition problem).

Error analysis when scoring DCPM can provide insight on the types of errors students are making on math probes, and better assist us in making an effective instructional match.
Putting DCPM in Context:
Norms, skill, administration time, growth
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Frustrational</td>
<td>Grades 1-3 &lt;10 DCPM</td>
<td>&lt;20 DCPM</td>
<td>Grades 2-3 &lt;14 DCPM, Grades 4-5 &lt;24 DCPM</td>
<td>Acquisition</td>
</tr>
<tr>
<td></td>
<td>Grades 4+ &lt;20 DCPM</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Instructional</td>
<td>Grades 1-3 10-19 DCPM</td>
<td>20-30 DCPM</td>
<td>Grades 2-3 14-31 DCPM, Grades 4-5 24-49 DCPM</td>
<td>Fluency</td>
</tr>
<tr>
<td></td>
<td>Grades 4+ 20-39 DCPM</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mastery</td>
<td>Grades 1-3 20+ DCPM</td>
<td>40+ DCPM</td>
<td>Grades 2-3 32+ DCPM, Grades 4-5 50+ DCPM</td>
<td>Maintenance; Generalization; Adaptation</td>
</tr>
<tr>
<td></td>
<td>Grades 4+ 40+DCPM</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Early numeracy assessments by skill area</td>
<td>Assessment</td>
<td>Skill</td>
<td>Time</td>
<td>Mastery</td>
</tr>
<tr>
<td>----------------------------------------</td>
<td>---------------------</td>
<td>------------------------</td>
<td>----------</td>
<td>---------</td>
</tr>
<tr>
<td><strong>Gateway skills:</strong> A foundational piece to understanding quantity is acquiring gateway skills. These include counting skill, number recognition, and writing numbers. These skills are needed to support the development of concepts aligned with number sense such as correspondence, cardinality, and quantitative relationships.</td>
<td>Oral counting</td>
<td>Rote counting</td>
<td>1 minute</td>
<td>80 DCPM</td>
</tr>
<tr>
<td></td>
<td>Number identification</td>
<td>Symbol recognition</td>
<td>1 minute</td>
<td>60 DCPM</td>
</tr>
<tr>
<td></td>
<td>Number writing</td>
<td>Symbol production</td>
<td>1 minute</td>
<td>60 DCPM</td>
</tr>
<tr>
<td><strong>Number Sense:</strong> Students develop skills to describe, compare, and manipulate numbers and their associated quantities. Students expand math-related vocabulary to perform and describe these tasks across contexts.</td>
<td>Missing number</td>
<td>Counting from number</td>
<td>1 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>Quantity discrimination</td>
<td>Number comparison</td>
<td>1 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td><strong>Number combinations:</strong> Students combine gateway and number sense skills, and write and solve basic number sentences to represent the manipulation of quantity.</td>
<td>Number combinations: addition</td>
<td>Addition: Sums to 10</td>
<td>1 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>Number combinations: Subtraction</td>
<td>Subtraction: Sums from 10</td>
<td>1 minute</td>
<td>20 DCPM</td>
</tr>
</tbody>
</table>

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<table>
<thead>
<tr>
<th>Probe set</th>
<th>Skill</th>
<th>Problem type(s)</th>
<th>Time</th>
<th>Mastery</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic fact computation</td>
<td>+</td>
<td>0 + 0 to 9 + 9</td>
<td>1 minute</td>
<td>40 DCPM</td>
</tr>
<tr>
<td></td>
<td>-</td>
<td>0 - 0 to 18 - 9 single-digit answers</td>
<td>1 minute</td>
<td>40 DCPM</td>
</tr>
<tr>
<td></td>
<td>×</td>
<td>0 x 0 to 9 x 9</td>
<td>1 minute</td>
<td>40 DCPM</td>
</tr>
<tr>
<td></td>
<td>÷</td>
<td>0 ÷ 0 to 81 ÷ 9 single-digit answers</td>
<td>1 minute</td>
<td>40 DCPM</td>
</tr>
<tr>
<td>Mixed computation</td>
<td>+</td>
<td>Mixed addition</td>
<td>3 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>-</td>
<td>Mixed subtraction</td>
<td>3 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>×</td>
<td>Mixed multiplication</td>
<td>3 minute</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>÷</td>
<td>Mixed division</td>
<td>3 minute</td>
<td>20 DCPM</td>
</tr>
</tbody>
</table>

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<table>
<thead>
<tr>
<th>Skill</th>
<th>Problem type(s)</th>
<th>Time</th>
<th>Mastery</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multidigit addition</td>
<td>+ 3 x 3 digit</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>+ 2 x 1 digit with regrouping</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>+ 3 x 3 digit with regrouping</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td>Multidigit subtraction</td>
<td>- 3 x 3 digit</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>- 2 x 1 digit with regrouping</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>- 3 x 3 digit with regrouping</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td>Multidigit multiplication</td>
<td>x 2 x 1 digit</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>x 4 x 2 digit</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>x 4 x 3 digit</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td>Multidigit division</td>
<td>÷ 3 ÷ 1 digit no remainder</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>÷ 3 ÷ 1 digit with remainder</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
<tr>
<td></td>
<td>÷ 3 ÷ 1 digit with decimals</td>
<td>2 minutes</td>
<td>20 DCPM</td>
</tr>
</tbody>
</table>

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<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>20</td>
<td>0.3</td>
<td>0.5</td>
</tr>
<tr>
<td>2</td>
<td>Mastery: More than 31, Instructional: 14-31, Frustration: Less than 14</td>
<td>0.3</td>
<td>0.5</td>
</tr>
<tr>
<td>3</td>
<td>Mastery: More than 31, Instructional: 14-31, Frustration: Less than 14</td>
<td>0.3</td>
<td>0.5</td>
</tr>
<tr>
<td>4</td>
<td>Mastery: More than 49, Instructional: 24-49, Frustration: Less than 24</td>
<td>0.75</td>
<td>1.2</td>
</tr>
<tr>
<td>5</td>
<td>Mastery: More than 49, Instructional: 24-49, Frustration: Less than 24</td>
<td>0.75</td>
<td>1.2</td>
</tr>
<tr>
<td>6</td>
<td>Mastery: More than 79, Instructional: 40-79, Frustration: Less than 40</td>
<td>0.45</td>
<td>1.0</td>
</tr>
</tbody>
</table>
It was found that the average growth rate across sessions of intervention was 1.62 DCPM, and across blocks of 15 min of instructional time was 3.58 DCPM for single-case research designs.

Interventions Included: Cover Copy Compare, Concrete, Representational Abstract, Detect Practice Repair, Explicit Timing, Math to Mastery, Taped Problems

<table>
<thead>
<tr>
<th>IF Learning Hierarchy</th>
<th>Acquisition</th>
<th>Proficiency</th>
<th>Generalization</th>
<th>Adaption</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haven’t had enough help</td>
<td>Haven’t had enough practice</td>
<td>Haven’t had to do it that way before</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Stages of Learning Computation

Acquisition  Proficiency  Mastery
Performance Improving
Errors Decreasing

Generalization Adaptation Maintenance
Stages of Learning Computation

- Explicit Modeling
- Guided Practice
- Independent Practice
- Performance Improving
- Errors Decreasing
- Acquisition
- Proficiency
- Mastery
- Generalization Adaptation Maintenance
What strategies are effective for students in the acquisition stage?

- Teacher actively demonstrates target skill
- Teacher uses ‘think-aloud’ strategy—especially for thinking skills that are otherwise covert
- Student has models of correct performance to consult as needed (e.g., correctly completed math problems on board)
- Student gets feedback about correct performance
- Student receives praise, encouragement for effort

(“The Instructional Hierarchy: Linking Stages of Learning to Effective Instructional Techniques | Intervention Central,” 2020)
What strategies are effective for students in the fluency stage?

- Teacher structures learning activities to give student opportunity for active (observable) responding
- Student has frequent opportunities to drill (direct repetition of target skill) and practice (blending target skill with other skills to solve problems)
- Student gets feedback on fluency and accuracy of performance
- Student receives praise, encouragement for increased fluency

(“The Instructional Hierarchy: Linking Stages of Learning to Effective Instructional Techniques | Intervention Central,” 2020)
What strategies are effective for students in the generalization/maintenance stage?

- Teacher structures academic tasks to require that the student use the target skill regularly in assignments.
- Student receives encouragement, praise, reinforcers for using skill in new settings, situations
- If student confuses target skill with similar skill(s), the student is given practice items that force him/her to correctly discriminate between similar skills
- Teacher works with parents to identify tasks that the student can do outside of school to practice target skill
- Student gets periodic opportunities to review, practice target skill to ensure maintenance

*The Instructional Hierarchy: Linking Stages of Learning to Effective Instructional Techniques. Intervention Central (2020)*
Instructional Intensification
<table>
<thead>
<tr>
<th>Dimension of Intensity</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strength</td>
<td>How well the program works for students with intensive intervention needs (what is effect size?)</td>
</tr>
<tr>
<td>Dosage</td>
<td># of opportunities a student has to respond and receive corrective feedback</td>
</tr>
<tr>
<td>Alignment</td>
<td>How well the program (a) addresses the target student’s full set of academic skill deficits, (b) does not address skills the target student has already mastered (extraneous skills for that student), and (c) incorporates a meaningful focus on grade-appropriate curricular standards</td>
</tr>
<tr>
<td>Attention to Transfer</td>
<td>The extent to which an intervention is designed to help students (a) transfer the skills they learn to other formats and contexts and (b) realize connections between mastered and related skills</td>
</tr>
<tr>
<td>Comprehensiveness</td>
<td># of explicit instruction principles the intervention incorporates</td>
</tr>
<tr>
<td>Behavioral Support</td>
<td>program incorporates (a) self-regulation and executive function components and (b) behavioral principles to minimize non-productive behavior</td>
</tr>
<tr>
<td>Individualization</td>
<td>A validated, data-based process for process for individualizing intervention, with which the special educator systematically adjusts an intensive intervention platform over time to address the student’s complex learning needs</td>
</tr>
</tbody>
</table>

Adapted from: Fuchs, Fuchs & Malone (2017), *The Taxonomy of Intervention Intensity*, *Teaching Exceptional Children* (50), 35-43.
When do we intensify intervention?

Student need persists despite:

- Intervention implementation with fidelity and for appropriate frequency/duration
- Evidence of effectiveness with similar students
- Use of a valid and reliable progress-monitoring tool that is sensitive to student change and matched to the correct measurement outcome
Intervention is aligned to grade-level curriculum if it:
Provides instruction for prerequisite skills required for content taught in core instruction.
Allows students to practice the grade-level skill on instructional-level text.
Provides more opportunities to respond and receive feedback on grade-level skills.

An intervention would **not be aligned to the grade-level curriculum if it:**
Provides instruction on some skills but neglects others.
Replaces core instruction so that students do not have the opportunity to develop background knowledge, vocabulary, and so on from grade-level content.
Key Features of Tier 2 & 3 Mathematics Intervention

- Explicit Instruction
- Strategy Instruction
- Sequencing Instruction
- Ongoing Progress Monitoring & Feedback
- Drill, practice & cumulative review
- Student verbalization
- Visual representation
- Motivation + Reinforcement

Codding, Volpe & Poncy (2016)
Interventions
<table>
<thead>
<tr>
<th>Intervention</th>
<th>Skill(s) Targeted</th>
<th>Individual, Small Group, Classwide Intervention</th>
<th>Time / Dosage</th>
<th>Learning Stage / Instructional Hierarchy</th>
</tr>
</thead>
<tbody>
<tr>
<td>The Great Race</td>
<td>Counting, cardinality (1-10)</td>
<td>Individual, small group</td>
<td>15 minutes (individual) or 25 minutes (small group) 2 x per week for 2 weeks</td>
<td>Fluency</td>
</tr>
<tr>
<td>Race to Space</td>
<td>Counting, cardinality (1-100)</td>
<td>Individual, small group</td>
<td>15 minutes (individual) or 25 minutes (small group) 2 x per week for 2 weeks</td>
<td>Fluency</td>
</tr>
<tr>
<td>Concrete – Representational-Abstract (CRA)</td>
<td>Conceptual understanding, language / vocabulary, procedural skills for early numeracy, addition, subtraction, multiplication, division, fractions, integers, equations</td>
<td>Individual, small group, classwide</td>
<td>Varied dependent upon skill</td>
<td>Acquisition</td>
</tr>
<tr>
<td>Incremental Rehearsal</td>
<td>Basic math facts (addition, subtraction, multiplication, division) Numerical identification</td>
<td>Individual</td>
<td>10-20 minutes per session 2x per week for 4-12 weeks</td>
<td>Acquisition - Fluency</td>
</tr>
<tr>
<td>Math to Mastery</td>
<td>Computation (addition, subtraction, multiplication, division)</td>
<td>Individual</td>
<td>10-minute sessions 3 to 5 times weekly for 3 to 8 weeks</td>
<td>Acquisition - Fluency</td>
</tr>
<tr>
<td>Drill Sandwich</td>
<td>Basic math facts (addition, subtraction, multiplication, division) Numerical identification</td>
<td>Individual “could be adapted for partner work”</td>
<td>10-20 minutes per session 2x per week for 4-12 weeks</td>
<td>Fluency</td>
</tr>
<tr>
<td>Classwide Fluency Building</td>
<td>Numbers and operations, computation skills, word problem solving, procedural fluency</td>
<td>Classwide</td>
<td>Approximately 10-15 minutes daily</td>
<td>Fluency</td>
</tr>
<tr>
<td><strong>Cover-Copy-Compare</strong></td>
<td><strong>Computation skills</strong></td>
<td><strong>Individual, small group, classwide</strong></td>
<td><strong>3-10 minutes daily 2 to 5 sessions per week 2 to 16 weeks</strong></td>
<td><strong>Fluency</strong></td>
</tr>
<tr>
<td>------------------------</td>
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</tr>
<tr>
<td><strong>Detect-Practice-Repair</strong></td>
<td><strong>Computation skills</strong></td>
<td><strong>Individual, small group, classwide</strong></td>
<td><strong>10-12 minutes daily</strong></td>
<td><strong>Fluency  *works best for students with higher fluency skills on target skill than those who are dysfluent*</strong></td>
</tr>
<tr>
<td><strong>Taped Problems</strong></td>
<td><strong>Math facts: simple and complex computation problems (addition, subtraction, multiplication, division)</strong></td>
<td><strong>Individual  *Adapted for Classwide w/ added group contingency</strong></td>
<td><strong>8-15 minutes per session, 3 to 5 times per week for 3 to 10 weeks</strong></td>
<td><strong>Fluency</strong></td>
</tr>
<tr>
<td><strong>Explicit Timing</strong></td>
<td><strong>Addition, subtraction &amp; multiplication (single and multi-digit)</strong></td>
<td><strong>Small group, classwide</strong></td>
<td><strong>3-10 minute sessions 2 to 5 times per week 4 to 6 total weeks</strong></td>
<td><strong>Fluency</strong></td>
</tr>
<tr>
<td><strong>High-Preference / Interspersed Problems</strong></td>
<td><strong>Complex computation including addition and subtraction with regrouping</strong></td>
<td><strong>Individual, small group, classwide</strong></td>
<td><strong>10 minutes daily 3 to 5 times per week For 3 to 5 weeks</strong></td>
<td><strong>Fluency - Generalization</strong></td>
</tr>
</tbody>
</table>

\*Classwide intervention is most effective when delivered 4-5 times per week.*
Acquisition Interventions
What best describes your interest in spending more time on each of the following? Stamp once for each:

<table>
<thead>
<tr>
<th>Strategy</th>
<th>Full Plate!!!</th>
<th>Just Dessert Please</th>
<th>I want to go home!</th>
</tr>
</thead>
<tbody>
<tr>
<td>CRA</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Math to Mastery</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Incremental Rehearsal</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Math Vocabulary</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word Problems</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Concrete - Representational - Abstract

Intentionally scaffolding to make concepts/procedures more explicit
Concrete – Representational - Abstract

Routine

1. Develop the CRA progression
   a) Outline the thought/language requirements of the abstract problem.
   b) Select/develop modeling structure that can be used with object and easily drawn.
   c) Determine the manipulative(s) to be used.
   d) Establish connections between the three models
2. Teach Concrete Model
   a) Teach the manipulative
   b) Ensure correct language/thought process
3. Teach Representational Model
   a) Build efficiency with modeling and language
   b) Increase complexity of problems
4. Teach Abstract Model
   a) Build understanding from concrete and representational models
   b) Utilize language to think aloud
5. Ongoing Progress Monitoring
   a) Develop a task analysis in line with the math concept/procedure
   b) Assess student on the process and provide corrective feedback
   c) Transition through CRA progression as students demonstrate understanding.

When to use?

Use this intervention if:
- Student struggles with underlying concepts
- Student struggles with math language
- Student struggles with math facts
- Student needs support with procedural skills

Example Activity

Overview

Resources
Addition Overview

C

R

A

\[
\begin{align*}
1 & \quad 5 \quad 2 \quad 5 \\
+ & \quad 1 \quad 3 \quad 6 \\
\hline
& \quad 6 \quad 6 \quad 1
\end{align*}
\]
Equivalence Overview

C

R

A

\[
\begin{align*}
\frac{2 \times 3}{3 \times 3} & = \frac{6}{9}
\end{align*}
\]
Adding and Subtracting Integers

\[ a \pm b \]

Concrete

 Representation

Abstract

\[-3 + 5 = 2\]
- Teacher-directed intervention for individual students
- Computation skills (researched on addition-can be applied to other operations)
- Teacher drills down to earliest prerequisite skill for intervention
- 1-minute trials to mastery (e.g., 32 dcpm) or maximum of 10 1-minute trials

Doggett, Hennington, & Johnson-Gros (2006)
1. Determine the skill(s) used for the intervention according to CBA or computer adapted assessments.
   a) The earliest unmastered pre-requisite skills in the sequence for the math operation should be targeted first.
2. Demonstrate how to complete each math problem on a worksheet while the student follows along on his/her copy.
3. Student practices the problems on the worksheet in one-minute trials until mastery criterion (e.g., 32 DCPM) is attained or ten one-minute trials are completed.
4. Follow along while student is working, marking errors and giving immediate corrective feedback.
5. After each one-minute trial, compute the digits correct and errors; provide specific praise for effort and performance.
6. Student charts his/her performance at the end of each 1-minute trial.
7. At the end of each session (or at least once weekly), student is administered a brief assessment (e.g., CBA), which is completed individually and scored to monitor progress on the target skill.
8. Once every other week (or monthly), a multiple skill CBM probe is administered to progress monitor for generalization.

Use this intervention if:
- Student is having difficulty with computation skills (addition, subtraction, multiplication, division)

**Math to Mastery**

**Routine**

**When to use?**

**Example Activity**

**Resources**


Incremental Rehearsal

- Teacher-directed intervention for individual students
- Computation skills acquisition moving toward fluency
  
  **Strong effect size: 1.67** (Burns, Zaslofsky, Kanive, & Parker, 2012)

- Assess for known and unknown facts
- 9 knowns to 1 unknown (90% known to 10% unknown)
1. Develop the flashcard sets of known and unknown items
   a) Assess the student by showing them each of the cards one at a time.
   b) If the student responds orally with the correct fact within 2 seconds, place the flashcard in the
      known items pile
   c) If the student gives an incorrect response, no response, or a correct response after 2 seconds,
      place the flashcard in the unknown item pile.
   d) To prepare for the intervention, select 9 known items and 1 unknown item. The rest of the
      known items will not be used.

2. Run first intervention trial
   a) Present the unknown item. Read the problem and the answer. Student repeats the problem
      and the answer.
   b) Present a known item. Student reads the problem and answer.
      • If student errors, teacher prompts with the correct fact and student repeats. Process is
        continued until student responds correctly to both the known and unknown items.
   c) Add another known item to the card stack. Repeat the process
   d) Continue until you have reached 9 known items and 1 unknown item.
   e) The unknown item is now considered a known item.

3. Run additional trial
   a) Begin with a new unknown item and the previous unknown item.

4. Session is ended when time runs out or student errors on unknown item three times.

Use this intervention if:
• Student is accurate, but slow with fact recall
• Student knows some facts, but not all facts.

Overview
Math Vocabulary

1. Exposure
2. Quick Teach
3. **Explicit Instruction** (Vocabulary Routine)
Step 1: Introduce the word

Step 2: Introduce the word’s meaning

Step 3: Illustrate the word with examples

Step 4: Check students’ understanding
  • Ask deep processing questions
  • Have students discern between examples and non-examples
  • Have students generate their own examples
  • Have students generate a sentence (using a sentence starter)
## Explicit Vocabulary Instruction

### Quadratic

<table>
<thead>
<tr>
<th>What is it?</th>
<th>What are the key features?</th>
</tr>
</thead>
<tbody>
<tr>
<td>A type of polynomial</td>
<td>Expression/equation must have $x^2$ or $x$'s being multiplied to give $x^2$</td>
</tr>
<tr>
<td>Can be expression, equation, or function</td>
<td>Graph is a parabola</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Example(s)</th>
<th>Non-example(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(x - 2)(x + 4)$</td>
<td>$2 = 3(x - 1)$</td>
</tr>
<tr>
<td>$x^2 - 2x + 3$</td>
<td>$x^3 - 2x^2$</td>
</tr>
<tr>
<td>$x^2 - 2x + 3 = 8$</td>
<td>$(2 - 3)(x - 1)$</td>
</tr>
</tbody>
</table>
Students must practice using the vocabulary!

- Word banks & Word walls
- Sentence starters
- Discussion (peer tutoring)
- Writing
- Reading
Word Problems

1. Attack Strategy
2. Schema-based Instruction
UPS- ✔
Understand
Plan
Solve
Check

Example: Cognitive Strategy Instruction
Sienna has $70 more than Paul. Paul has $45. How much money does Sienna have?

\[ G - L = D \]

\[ G - 45 = 70 \]

\[ G = 115 \]

<table>
<thead>
<tr>
<th>Greater</th>
<th>Lesser</th>
<th>Difference</th>
</tr>
</thead>
<tbody>
<tr>
<td>$45</td>
<td>$70</td>
<td>$70</td>
</tr>
</tbody>
</table>

Sienna
Schema-Based Problem Solving

Additive Schema
1. Total
2. Difference
3. Change

Multiplicative Schema
1. Equal Groups
2. A Set Multiplied
3. Ratios/Proportions
Which intervention are you most likely to use?
How might you support others to implement these interventions?
Break time!

Next session at 10:45
Strategic and Intensive Interventions in Mathematics - Part 2 of 2

Dr. Erica Kaurudar, NCSP
Mr. Jared Campbell
Dr. Drew Hunter
Pennsylvania Training and Technical Assistance Network
Highlights:

Part 1
- Diagnostic Assessment for Intervention Selection
- Instructional Hierarchy
- Intensification and features of math interventions
- Acquisition Interventions

Part 2
- Fluency Interventions
- Progress Monitoring
- Decision Making
Let’s Stamp!
Let’s practice!
Where did you do your school psych training?

Not in PA:
What best describes your role? You may stamp more than one if it applies to you.

<table>
<thead>
<tr>
<th>Graduate Student</th>
<th>Higher Ed Faculty</th>
<th>K-12 School Psych Practitioner</th>
<th>Specialized Setting School Psych Practitioner</th>
<th>Administrator</th>
<th>Other</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Fluency Interventions
<table>
<thead>
<tr>
<th>IF</th>
<th>Acquisition</th>
<th>Proficiency</th>
<th>Generalization</th>
<th>Adaption</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Learning Hierarchy</strong></td>
<td>Haven’t had enough help</td>
<td>Haven’t had enough practice</td>
<td>Haven’t had to do it that way before</td>
<td></td>
</tr>
<tr>
<td><strong>Instructional Hierarchy</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Mathematics Interventions Aligned to Learning Stages / Instructional Hierarchy</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Intervention</strong></td>
</tr>
<tr>
<td>---</td>
</tr>
<tr>
<td><strong>The Great Race</strong></td>
</tr>
<tr>
<td><strong>Race to Space</strong></td>
</tr>
<tr>
<td><strong>Concrete – Representational–Abstract (CRA)</strong></td>
</tr>
<tr>
<td><strong>Incremental Rehearsal</strong></td>
</tr>
<tr>
<td><strong>Math to Mastery</strong></td>
</tr>
<tr>
<td><strong>Drill Sandwich</strong></td>
</tr>
<tr>
<td><strong>Classwide Fluency Building</strong></td>
</tr>
<tr>
<td>Intervention</td>
</tr>
<tr>
<td>----------------------------</td>
</tr>
<tr>
<td><strong>Cover-Copy-Compare</strong></td>
</tr>
<tr>
<td><strong>Detect-Practice-Repair</strong></td>
</tr>
<tr>
<td><strong>Taped Problems</strong></td>
</tr>
<tr>
<td><strong>Explicit Timing</strong></td>
</tr>
<tr>
<td><strong>High-Preference / Interspersed Problems</strong></td>
</tr>
</tbody>
</table>

*Classwide intervention is most effective when delivered 4-5 times per week.*
What best describes your interest in spending more time on each of the following? Stamp once for each:

<table>
<thead>
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<tbody>
<tr>
<td>The Great Race</td>
<td></td>
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</tr>
<tr>
<td>Race to Space</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cover – Copy - Compare</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Detect – Practice – Repair</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Explicit Timings</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
1. Construct a gameboard of 10 horizontally-arranged squares of equal size with numbers 1-10 listed left to right. Ensure “start” is by 1 and “end” is by 10.
2. Create a game spinner by dividing a circle in two halves. One half labeled “1” and the other half labeled “2.”
3. Find items for game pieces representing different colors / shapes (e.g., buttons, beads).
4. Student and teacher each select their game piece.
5. Tell student that you will each take turns spinning the spinner. Whomever reaches the end first wins.
6. Tell the student when it is her turn that he should move his game piece the number of spaces indicated on the spinner (either 1 or 2 spaces).
7. Ask the student to say the number she spun AND to say the numbers on the spaces through which she moved.
   a. For example, if the student was on the numeral 5 and spun 2, she should say, “I am on number 5 and spun a 2, so I will move two spaces.” The student should say, “six, seven” as she moved her game piece.
8. If the student names the numeral incorrectly, provide the student with the correct number and have him repeat the name(s) while moving the token.

The Great Race

Use this intervention if:
Student needs practice with counting and cardinality

When to use?

Example Activity

Resources

Game Board for The Great Race

The Great Race

START

1 2 3 4 5 6 7 8 9 10

END
1. Construct a gameboard of 10x10 matrix of squares of equal size with numbers 1-100 arranged from the bottom left (1) to the top right (100). Place the word start with the numeral “0” beside it at the beginning, and place a star or the word “end” by the numeral 100. Background of board gradually darkens as numerals increase, providing a cue for number magnitude.

2. Create a game spinner by dividing a circle into 5 equal sections labeled 1 to 5.

3. Find items for game pieces representing different colors / shapes (e.g., buttons, beads).

4. Student(s) and teacher each select their game piece.

5. Tell students that the purpose of the game is to learn about the numbers 0 to 100. Explain you will each take turns spinning the spinner. Whomever reaches the end first wins.

6. Tell the student when it is her turn that he should move his game piece the number of spaces indicated on the spinner (either 1 or 2 spaces).

7. Ask the student to say the number she spun AND to say the numbers on the spaces through which she moved.
   a. For example, if the student was on the numeral 5 and spun 2, she should say, “I am on number 5 and spun a 2, so I will move two spaces.” The student should say, “six, seven” as she moved her game piece.

8. If the student names the numeral incorrectly, provide the student with the correct number and have him repeat the name(s) while moving the token.

Use this intervention if:
Student needs practice with counting and cardinality

Example Activity


## Game Board for Race to Space

### Race to Space

<table>
<thead>
<tr>
<th>91</th>
<th>92</th>
<th>93</th>
<th>94</th>
<th>95</th>
<th>96</th>
<th>97</th>
<th>98</th>
<th>99</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>81</td>
<td>82</td>
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<td>16</td>
<td>17</td>
<td>18</td>
<td>19</td>
<td>20</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>8</td>
<td>9</td>
<td>10</td>
</tr>
</tbody>
</table>

0Start
1. Develop the Cover-Copy-Compare sheet.
   a) Section a worksheet into three columns.
   b) Select up to 10 facts for students to practice.
   c) Write the facts as correct models on the left column. (You could use the right column if the student is left handed.)

2. Student completes the sheet
   a) Study the correct fact, practice saying it the fact.
   b) Cover the fact. (by hand or by folding the paper)
   c) Copy the fact in the next column while saying the fact.
   d) Uncover the original, and compare.
      - If correct move to next problem
      - If incorrect, cross out the incorrect fact and go to step 2a.
   e) Continue until all facts are complete.

3. Update records/graphs
   a) If student correctly complete a facts for 3 consecutive trials
      - Update their known facts list to include this item
      - Update graph to monitor progress

Variation: Instead of writing the facts, students can practice verbal responses.

Use this intervention if:
- Student is struggling to acquire new math facts.
- Student is not maintaining accuracy with previously know math facts.
- Student is able to replicate the process independently.

Example Activity

Overview
http://www.intensiveintervention.org/chart/instructional-intervention-tools

Known Facts Lists
## Cover-Copy-Compare Materials

<table>
<thead>
<tr>
<th>Math Facts</th>
<th>Student Response</th>
</tr>
</thead>
<tbody>
<tr>
<td>8 + 1 = 9</td>
<td></td>
</tr>
<tr>
<td>9 x 8 = 72</td>
<td></td>
</tr>
<tr>
<td>16 - 8 = 8</td>
<td></td>
</tr>
<tr>
<td>2 + 6 = 8</td>
<td></td>
</tr>
<tr>
<td>2 x 4 = 8</td>
<td></td>
</tr>
</tbody>
</table>

**Worksheet: Cover-Copy-Compare**

**Student:**

**Date:**
1. Detect unknown items
   a) Give students a structured sheet to record their answers.
   b) *Present math fact for 3 seconds, while student writes the answer on their sheet.
   c) Repeat for set of targeted math facts.
   d) At the end of the assessment, display the answer key and have students identify incorrect responses.

2. Practice
   a) Student develops their own CCC sheet
      • Use correct version of their first 5 errors.
   b) Perform CCC procedure.

3. Repair
   a) Teacher provides feedback.
   b) CCC can be repeated.
   c) Other fluency interventions can be applied for additional practice.

Variation(s): Can use a timer and flashcards or PPT and 3 second transitions. Prompts could be provided verbally instead of visually.

* If using PPT for facts, set the transition duration to 3 seconds.

When to use?

Use this intervention if:
- Student knows some facts, but not all facts.
- Working with a group of students.
- Cover-Copy-Compare is already in use.
- Need to individualize CCC routine.

Example Activity

Resources


Cover-Copy-Compare Materials

Detect-Practice-Repair Variation with PowerPoint:

Worksheet: Cover-Copy-Compare

<table>
<thead>
<tr>
<th>Math Facts</th>
<th>Student Response</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. ( \frac{8}{9} + 1 )</td>
<td>1a. ( \frac{8}{9} ) 1b. ( \frac{8}{9} + 1 )</td>
</tr>
<tr>
<td>2. ( 9 \times 8 )</td>
<td>2a. ( 9 \times 8 ) 2b. ( 9 \times 8 )</td>
</tr>
<tr>
<td>3. ( \frac{16}{8} - 8 )</td>
<td>3a. ( \frac{16}{8} - 8 ) 3b. ( \frac{16}{8} - 8 )</td>
</tr>
<tr>
<td>4. ( 2 + 6 )</td>
<td>4a. ( 2 + 6 ) 4b. ( 2 + 6 )</td>
</tr>
<tr>
<td>5. ( \frac{2}{4} \times 8 )</td>
<td>5a. ( \frac{2}{4} \times 8 ) 5b. ( \frac{2}{4} \times 8 )</td>
</tr>
</tbody>
</table>
Explicit Timing

**Routine**

1. Select skill on which student will practice
   a) Develop appropriate skill sequence
   b) Access appropriate practice worksheets
   c) Assess and identify the starting skill
2. Document date, start time, & end time
3. Pass out worksheets or Explicit Timing folder.
4. If doing self graphing, read the following, “class, please open your folder and locate your graph and score from yesterday’s practice. Mark your score on your graph and see whether you beat your previous score (pause). Now take out today’s math worksheet”.
5. Read directions, “Today we are going to complete math worksheets using explicit timing. With explicit timing I am going to give you x minutes to complete as many problems as you can. Your first goal is to complete each problem correctly and to not skip around. In addition push yourself to work as quickly as possible. Ready, begin”.
6. Start stopwatch and stop students after x minutes have elapsed.
7. Score probes to inform decision making
   1. Move back a skill (student is inaccurate)
   2. Continue with current skill (student is accurate)
   3. Move to next skill (student has eclipsed mastery criteria)

**When to use?**

Use this intervention if:
1. Student has accurate responding
2. Student has not yet developed fluency

**Example Activity**

**Resources**


http://www.otiss.net/interventions/explicit-timing/
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Which intervention are you most likely to use?
How might you support others to implement these interventions?
We will look very briefly at evaluating student response to intervention through the lens of Rate of Improvement (ROI), Student Growth Percentiles (SGPs), and Mastery Measurement.
What progress monitoring tool does your district use for math?

<table>
<thead>
<tr>
<th>DIBELS or Acadience Math</th>
<th>STAR Math</th>
<th>AIMSWeb Plus</th>
<th>Spring Math</th>
<th>NA- Graduate Student</th>
<th>Other (or none, or it’s complicated)</th>
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Progress monitoring is a rigorous assessment technique based on research on applications of repeated measurement techniques featuring brief and frequent measurements.

Important part of the progress monitoring process is the evaluation of student performance over time.

Examples: AIMSWeb, DIBELS, Star
Important part of the progress monitoring process is the evaluation of student performance over time.

Behavior over time is reflected in rate of change or slope.

Slope calculation needs to be for typical/benchmark performance as well as the expected and actual levels of the student's performance.
Important Terms:

**Typical ROI** = From benchmark to benchmark

**Target ROI** = From starting score of student to benchmark of typical benchmark

**Attained ROI** = From starting score of student to ending score of student

Shapiro (2011)
Grade 2 Student – How Low? How Slow? Example

Typical Benchmark ROI = 0.67 pts/wk

Target Benchmark ROI = 1.00 pts/wk

Attained Benchmark ROI = 0.31 pts/wk
Results - Benchmark ROI

- Typical ROI
  - Fall to Spring
  - pts/wk
  - \( \frac{(40 - 16)}{36} = 0.67 \)

- Target
  - Fall to Spring
  - pts/wk
  - \( \frac{(40 - 4)}{36} = 1.00 \)

- Attained ROI
  - Fall to Spring
  - pts/wk
  - \( \frac{(15 - 4)}{36} = 0.31 \)

- Student making progress over time (increasing)
- Student moving at slower rate than typical peers
- Student NOT closing the gap between

Shapiro
Best Practice: Ordinary Least Squares (OLS) aka Progress Monitoring ROI

Uses **linear regression**
- Mathematical process for establishing the straight line that cuts through ALL the data points & establishes LINEAR TREND in the data
- **AIM** line (expected performance) **TREND** line (actual performance)
- Takes into account ALL data points in the series
- Requires mathematical calculation (let software do it)!
- Some software (e.g., DIBELS, AIMSWeb) has capability to calculate it for you
- EXCEL can do it too!
Exampl

OLS / Progress

Monitoring

ROI

Sample PM from STAR Math

Angelina's Current Goal

Goal: 616 SS 54 PR (Moderate)  
Goal End Date: 6/2/2012  
Expected Growth Rate: 3.4 SS/week
Student Growth Percentiles (SGPs)

Student Growth Percentiles (SGPs) are calculated from triannual (3 x year) assessments and provide a normative comparison of growth to a student’s academic peers (e.g., students who started at the same/similar level).

Reported as percentile rank. Example: SGP of 50 is interpreted to indicate the student’s growth was equal or better than 50% of academically-like peers. (Examples: Acadience, AIMSWeb)
SGPs and Descriptors

- Very low: 1st to 10th percentiles
- Low: 11th to 25th percentiles
- Average: 26th to 74th percentiles
- High: 75th to 89th percentiles
- Very high: 90st to 99th percentiles
Figure 1  Fall and Spring Number Correct Scores, Number Naming Fluency
Figure 2  Growth by Initial Performance Level

Words Correct Per Minute

Fall    Spring

Very Low
Average
Very High
**Insufficient** (SGP ≥ 50): The ROI is below average and will not improve the student’s percentile rank enough to sufficiently close the performance gap.

**Closes the gap** (SGP of 51–84): The ROI is above average and the goal score will improve the student’s percentile rank.

**Ambitious** (SGP of 85 –97): The ROI is well-above average and the goal score will substantially improve the student’s percentile rank.

**Extremely Ambitious** (SGP ≤ 98): The ROI is greater than 97% of the ROIs in the national sample for students with a similar initial score and is rarely achieved in typical settings.
**Mastery Measurement:**

Measurement of student performance of a specific target skill

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www.interventioncentral.com
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Assessing Response to Intervention/Student Growth

Individual with Goal (Benchmark)
Peers with Goal (Benchmark)
Individual with Peers
Individual Growth: Goals for Austin

- Austin will increase levels in intervention at least every 4 weeks with intervention consistency score of at least 80%.

- Austin’s post-intervention performance will be in the not-at-risk range on the first goal skill for which he received intervention.

- Austin will perform outside of the risk range on subsequent screenings.
First Individual Intervention Skill, Adequate Growth
Second Individual Intervention Skill, Adequate Growth

Intervention Skill: Subtraction 0-9

Mastery Target (40)

Instructional Target (20)

Scores over time from December 31 to December 11.

Interventions for Fact Families: Add/Subtract 0-20 Daily Skill
- Sums to 12
- Subtraction 0-9
- Fact Families: Add/Subtract 0-9

Spring Math
Third Intervention Skill, Slow Growth: Met Mastery Goal with 9 weeks of Individual Intervention
Poor Generalization to Goal Skill. Inadequate Growth on the Goal Skill.
Student Progress Less Steep as compared to Classwide Median
What factors might need to be considered before making intervention adjustments?
- Was student present for 85% to 95% of intervention sessions?
- Was the intervention being delivered with the amount of time and intensity as planned?
- Were treatment integrity/fidelity data collected?
  - Direct observation of intervention
  - Review of permanent products
  - Interventionist self-report of completed steps

DiGenarro Reed & Codding, (2014)
Considerations Before Making Intervention Adjustments

- Was the student being provided with intervention in the correct level of instructional materials?
  - Correct subskill?
  - Learning stage considered? (e.g., acquisition, fluency, maintenance / generalization)

Riley-Tillman, Burns, & Gibbons (2013)
Evaluating Student Progress and Making Intervention Adjustments

**Little / No Improvement**
- Teach Prerequisite Skill
- Change Assistance
- Change Grouping
- Change Intervention

**Slow Improvement**
- Increase Dose
- Change Assistance
- Modify Intervention

**Meets Goal Line**
- Make No Changes
- Reduce Assistance

**Exceeds Goal Line**
- Adjust Target Skill
- Fade Treatment Dose
- Remove and Monitor

Adapted from Codd, Volpe, & Poncy (2017).
Q & A

Let’s chat!
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